

Quarter 3

Applied Mathematical Concepts

Quarter 1	Quarter 2	Quarter 3	Quarter 4
Linear Programming, Organizing and Interpreting Data, Data Descriptions	Probability and Counting Rules, Probability Distributions	Normal Probability Distribution, Confidence Intervals, Financial Mathematics	Financial Mathematics (cont.), Logic, Boolean Algebra
August 6 2018 – October 5, 2018	October 15, 2018 – December 19, 2018	January 7, 2019 - March 8, 2019	March 18, 2019 – May 23, 2019
AM.A.LP.A.1	AM.D.CR.A.1	AM.D.ND.A.1	AM.G.L.A.1
AM.A.LP.A.2	AM.D.CR.A.2	AM.D.ND.A.2	AM.G.L.A.2
AM.A.LP.B.3	AM.D.CR.A.3	AM.D.CI.A.1	AM.G.L.A.3
AM.A.LP.B.4	AM.D.CR.A.4	AM.D.Cl.A.2	AM.G.L.A.4
AM.D.ID.A.1	AM.D.CR.A.5	AM.D.CI.A.3	AM.G.L.B.5
AM.D.ID.A.2	AM.D.CR.B.7	AM. A. PS. A.1	AM.G.L.B.6
AM.D.ID.A.3	AM.D.CR.B.8	AM.N.NQ.A.1	AM.G.L.B.7
AM.D.ID.A.4	AM.D.CR.B.9	AM.N.NQ.A.2	AM.G.L.B.8
AM. A. PS. A.1	AM.D.CR.B.10	AM.N.NQ.A.3	AM.A.LB.A.1
AM.D.CR.B.10	AM.D.ID.A.4	AM.N.NQ.A.4	AM.A.LB.A.2
	AM.D.ID.A.5	AM.N.NQ.B.5	AM.A.LB.B.3
	AM.D.ID.A.6	AM.N.NQ.B.6	AM.A.LB.B.4
	AM.D.ID.A.7	AM.N.NQ.B.7	AM.N.NQ.C.9
	AM. A. PS. A.1	AM.N.NQ.B.8	AM.N.NQ.C.10
		AM.N.NQ.C.9	AM.D.CI.A.1
		AM.N.NQ.C.10	AM.D.CI.A.2



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AM.D.CI.A.3 Tennessee Academic Standards for Mathematics



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Introduction

Destination 2025, Shelby County Schools' 10-year strategic plan, is designed not only to improve the quality of public education, but also to create a more knowledgeable, productive workforce and ultimately benefit our entire community.

What will success look like?

80% of seniors will be college-or career-ready

90% of students will graduate on time

100%
of college-or career-ready
graduates enroll in
post-secondary opportunities

In order to achieve these ambitious goals, we must collectively work to provide our students with high quality, college and career ready aligned instruction. The Tennessee State Standards provide a common set of expectations for what students will know and be able to do at the end of a grade. The State of Tennessee provides two sets of standards, which include the Standards for Mathematical Content and The Standards for Mathematical Practice. The Content Standards set high expectations for all students to ensure that Tennessee graduates are prepared to meet the rigorous demands of mathematical understanding for college and career. The eight Standards for Mathematical Practice describe the varieties of expertise, habits of mind, and productive dispositions that educators seek to develop in all students. The Tennessee State Standards also represent three fundamental shifts in mathematics instruction: **focus, coherence and rigor**.

Instructional Shifts for Mathematics

Focus

Coherence

Rigor

Procedural Fluency

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The **Standards for Mathematical Practice** describe varieties of expertise, habits of minds and productive dispositions that mathematics educators at all levels should seek to develop in their students. These practices rest on important National Council of Teachers of Mathematics (NCTM) "processes and proficiencies" with longstanding importance in mathematics education. Throughout the year, students should continue to develop proficiency with the eight Standards for Mathematical Practice. The following are the eight Standards for Mathematical Practice:

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of them.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

This curriculum map is designed to help teachers make effective decisions about what mathematical content to teach so that ultimately our students can reach Destination 2025. Throughout this curriculum map, you will see resources as well as links to tasks that will support you in ensuring that students are able to reach the demands of the standards in your classroom. In addition to the resources embedded in the map, there are some high-leverage resources around the content standards and mathematical practice standards that teachers should consistently access. For a full description of each, click on the links below.

Tennessee Mathematics Content Standards
Standards for Mathematical Practice
Literacy Skills for Mathematical Proficency
Tennessee Academic Standards for Mathematics



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Structure of the Standards

Structure of the TN State Standards include:

- Content Standards Statements of what a student should know, understand, and be able to do.
- Clusters Groups of related standards. Cluster headings may be considered as the big idea(s) that the group of standards they represent are addressing. They are therefore useful as a quick summary of the progression of ideas that the standards in a domain are covering and can help teachers to determine the focus of the standards they are teaching.
- **Domains** A large category of mathematics that the clusters and their respective content standards delineate and address. For example, Number and Operations Fractions is a domain under which there are a number of clusters (the big ideas that will be addressed) along with their respective content standards, which give the specifics of what the student should know, understand, and be able to do when working with fractions.
- Conceptual Categories The content standards, clusters, and domains in the 9th-12th grades are further organized under conceptual categories. These are very broad categories of mathematical thought and lend themselves to the organization of high school course work. For example, Algebra is a conceptual category in the high school standards under which are domains such as Seeing Structure in Expressions, Creating Equations, Arithmetic with Polynomials and Rational Expressions, etc.



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How to Use the Maps

Overview

An overview is provided for each quarter and includes the topics, focus standards, intended rigor of the standards and foundational skills needed for success of those standards.

Your curriculum map contains four columns that each highlight specific instructional components. Use the details below as a guide for information included in each column.

Tennessee State Standards

TN State Standards are located in the left column. Each content standard is identified as Major Content or Supporting Content (for Algebra I, Algebra II & Geometry only). A key can be found at the bottom of the map.

Content

This section contains learning objectives based upon the TN State Standards. Best practices tell us that clearly communicating measurable objectives lead to greater student understanding. Additionally, essential questions are provided to guide student exploration and inquiry.

Instructional Support & Resources

District and web-based resources have been provided in the Instructional Support & Resources columns. You will find a variety of instructional resources that align with the content standards. The additional resources provided should be used as needed for content support and scaffolding. The inclusion of vocabulary serves as a resource for teacher planning and for building a common language across K-12 mathematics. One of the goals for Tennessee State Standards is to create a common language, and the expectation is that teachers will embed this language throughout their daily lessons.



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Topics Addressed in Quarter

- Normal Probability Distribution
- Confidence Intervals and Sample Size
- Financial Mathematics

Overview

In this quarter students study normal probability distribution and continue to have the opportunity to apply concepts of probability and statistics to real-world situations. Students determine confidence intervals to begin to hypothesize if a large enough sample size has been taken to closely reflect the true mean of the population. Students conclude the quarter with the study of financial mathematics which includes interest, annuities, amortizations, loans, financial decision-making and other real-world problems involving finance.

TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUF	PPORT & RESOURCES	
Normal Probability Distribution (Allow approximately 2 weeks for instruction, review, and assessment)				
Cluster: Work with the normal distribution in real-world situations. AM.D.ND.A.1 Calculate the mean (expected value) and standard deviation of both a random variable and a linear transformation of a random variable. AM.D.ND.A.2 Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimate population percentages. Recognize that there are data sets for which such a procedure is not appropriate. Use calculators, spreadsheets,	How do all Normal distributions relate to each other? How can we find examples of normal distribution in real world scenarios? How does the z-score relate to the standard normal distribution? Objective(s) The student will: Identify distributions as symmetric or skewed. Identify the properties of a normal	Elementary Statistics Textbook (Bluman) 6-1 The Normal Distribution 6-2 Applications of the Normal Distribution 6-3 The Central Limit Theorem 6-4 The Normal Approximation to the Binomial Distribution Additional Resource(s) Elementary Statistics 7th edition Bluman (PowerPoints, Chapter PDF files, Solutions Manual, etc.)	Vocabulary (Chapter 6) central limit theorem, correction for continuity, negatively or left-skewed distribution, normal distribution, positively or right-skewed distribution, sampling distribution of sample means, sampling error, standard error of the mean, standard normal distribution, symmetric distribution, z value Elementary Statistics Textbook (Bluman) Statistics Today, pp. 300, 350 Critical Thinking Challenges, p. 352 Applying the Concepts, pp. 311, 324, 338, 346	



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TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUPPORT & RESOURCES	
and tables to estimate areas under the normal curve.	 distribution. Find the area under the standard normal distribution, given various z values. Find probabilities for a normally distributed variable by transforming it into a standard normal variable. Find specific data values for given percentages, using the standard normal distribution. Use the Central Limit Theorem to solve problems involving sample means for large samples. How do all Normal distributions relate to each other? 	Khan Academy: The Normal Distribution Khan Academy: Binomial Distribution Against All Odds Videos & Lessons: Normal Curves Against All Odds Videos & Lessons: Normal Calculations Against All Odds Videos & Lessons: Checking Assumption of Normality Khan Academy: Central Limit Theorem Task(s) SCS Math Task: Statistics - Cents & Central Limit Theorem Statistics Applet-Sampling Distributions Statistics Applet: Normal to Binomial TI Activities: Normal Distribution TI Activity: Intro to the Central Limit Theorem Accelerated GSE Pre-Calculus Tasks: Unit 8: Inferences & Conclusions from Data Colors of Skittles, p. 120 Pennies, p.142 The Gettysburg's Address, p. 156	Extending the Concepts, pp.313, 340, 347 Data Projects, pp. 353, 397
Confidence Intervals and Sample Size			
(Allow approximately 3 weeks for instruction, review, and assessment)			
Domain: Understand and Use Confidence Intervals Cluster: Work with confidence intervals in real-	How do you extend the idea of estimating a parameter to allow for	$\frac{\text{Elementary Statistics Textbook (Bluman)}}{\text{7-1 Confidence Intervals for the Mean When }\sigma}$ is Known	Vocabulary (Chapter 7): chi-square distribution, confidence interval, confidence level, consistent estimator, degrees



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world situations. AM.D.CI.A.1 Understand the meaning of confidence level, of confidence intervals, and the properties of confidence intervals. AM.D.CI.A.2 Construct and interpret a large sample confidence interval for a proportion and for a difference between two proportions. AM.D.CI.A.3 Construct the confidence interval for a mean and for a difference between two means. Domain: Problem Solving Cluster: Apply problem solving techniques to real-world situations. AM.A. PS.A.1 Apply problem solving strategies to real-world situations. Strategies include, but are not limited to: making orderly lists or tables, drawing diagrams, considering simpler problems, looking for patterns, working backwards, guess and check, using logical reasoning, etc.	 uncertainty? How do I interpret the margin of error of a confidence interval? How do I use a margin of error to find a confidence interval? How does sample size raise the confidence level for the true mean? Objective(s): The student will: Find the confidence interval for the mean when σ is known and sample size is large. Determine the minimum sample size for finding a confidence interval for the mean. Find the confidence interval for the mean when σ is unknown and sample size is small. Find the confidence interval for a proportion. Determine the minimum sample size for finding a confidence interval for a proportion. Find the confidence interval for a variance and a standard deviation using Chi-Square. 	7-2 Confidence Intervals for the Mean When or is Unknown 7-3 Confidence Intervals and Sample Size for Proportions 7-4 Confidence Intervals for Variances and Standard Deviations Additional Resource(s) Elementary Statistics 7th edition Bluman (PowerPoints, Chapter PDF files, Solutions Manual, etc.) Against All Odds Videos & Lessons: Confidence Intervals Khan Academy: Confidence Intervals Stat Trek STatistics Education Web Stats Modeling the World Task(s) SCS Math Task: Statistics- Confidence Interval SCS Math Task: Statistics- SAT Performance Accelerated GSE Pre-Calculus Tasks: Unit 8: Inferences & Conclusions from Data How Confident Are You? p.177 TI-Activities: Confidence Intervals	of freedom, estimation, estimator, interval estimate, maximum error of the estimate, point estimate, proportion, relatively efficient, estimator, <i>t</i> distribution, unbiased estimator Elementary Statistics Textbook (Bluman) Statistics Today, pp. 356, 395 Critical Thinking Challenges, p. 397 Speaking of Statistics, pp. 381, 385 Applying the Concepts, pp. 365, 373, 381, 390 Extending the Concepts, pp. 375, 383, 391 Data Projects, p. 397 TI-83/84 Step by Step, pp. 368, 376, 384, 391



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Financial Mathematics (Allow approximately 4 weeks for instruction, review, and assessment; Note that 1-2 weeks at the beginning of 4th quarter is allocated for any topics not completed during this period.)			
Cluster: Use financial mathematics to solve problems. AM.N.NQ.A.1 Define interest, compound interest, annuities, sinking funds, amortizations, annuities, future value, and present value. AM.N.NQ.A.2 Recognize the importance of applying a financial model to business. AM.N.NQ.A.3 Determine future value and present value of an annuity. AM.N.NQ.A.4 Determine the amortization schedule for an annuity and a home mortgage. AM.N.NQ.B.5 Apply financial mathematics to depreciation schedules. AM.N.NQ.B.6 Solve contextual problems involving financial decision-making. AM.N.NQ.B.7 Apply arithmetic and geometric sequences to simple and compound interest, annuities, loans, and amortization. AM.N.NQ.B.8 Solve problems in mathematics of finance involving compound interest using exponential and logarithmic techniques. AM.N.NQ.C.9 Know when to use transcendental functions to accomplish various application purposes such as predicting population growth AM.N.NQ.C.10 Use orders of magnitude estimates for determining an appropriate	 Essential Question(s): How do the economic, social, and political climates as well as personal skills play a role in the level of individual financial risk and impact spending and other financial decisions? What constitutes a wise financial decision, and how do you make educated choices about spending? What are the elements or criteria for a solid financial plan? What do individuals need to know in order to make informed decisions about incurring debt? Why is it important to understand the value, features, and planning process associated with saving and investing? How does someone choose the best investment and/or savings options to achieve financial security? Objective(s): The student will: Solve financial problems that involve simple interest. Solve problems involving compound interest. Find the future value of an annuity, and 	Advanced Algebra & Trigonometry (Coburn) 4.3 Logarithms and Logarithmic Functions 4.5 Applications from Business, Finance and Science 11.1 Sequences and Series 11.2 Arithmetic Sequences 11.3 Geometric Sequences Algebra & Trigonometry (Blitzer) 4.4 Exponential and Logarithmic Functions 4.5 Exponential Growth and Decay; Modeling Data 11.1 Sequences and Summation Notation 11.2 Arithmetic Sequences 11.3 Geometric Sequences 11.3 Geometric Sequences 11.4 Tennessee Finite Math Textbook (Maki & Thompson) 9-1 Interest Math Lab: Continuously Compounded Interest (p.322) 9-2 The Present Value of Future Payments 9-3 Time Payment, Amortization, and Mortgages 9-4 Evaluating Investment Options and Financial Decision Making	Important Terms & Concepts (TN Finite Math, Chapter 9) Amortization, annual percentage rate, annual percentage yield, annuitization, annuity, bond, common stock, compound interest, current yield, depreciation, dividend, future value, interest, notes, present value, present value of an annuity, purchase at a premium, at a discount, or at par, redemption date, redemption value or face value, return on investment, simple interest, sinking fund, stated interest rate, stock split, straight-line method, sum of a geometric series, yield to maturity



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TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUPPORT & RESOURCES
model for a contextual situation. Domain: Problem Solving Cluster: Apply problem solving techniques to real-world situations. AM.A. PS.A.1 Apply problem solving strategies to real-world situations. Strategies include, but are not limited to: making orderly lists or tables, drawing diagrams, considering simpler problems, looking for patterns, working backwards, guess and check, using logical reasoning, etc.	the amount of payments to a sinking fund. Find the future value of an annuity, and an installment payment on a loan. Solve real-world problems involving the mathematics of finance.	Chapter 9 – The Finance of Mathematics 9.1 Interest 9.2 Annuities and Future Value 9.3 Present Value of an Annuity; Amortization Additional Resource(s) Khan Academy: Orders of Magnitude Example 1 Khan Academy: Orders of Magnitude Example 2 Khan Academy: Sequences & Series Khan Academy: Finance and Capital Markets Khan Academy: Interest Basics Khan Academy: Compound Interest Basics Khan Academy: Credit Cards & Loans Finite Math Assessments Financial Math Lessons Georgia Virtual Learning (Mathematics of Finance) Khan Academy: Present Value 2 Khan Academy: Present Value 2 Khan Academy: Present Value 4 Khan Academy: Present Value 4 Khan Academy: Amortized Loans Khan Academy: Mortgage Loans
		The Math Forum: Financial Education in the



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TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUF	PPORT & RESOURCES
	•	Math Classroom	
		Foundations U (Activities, Tools, Articles)	
		Comap - A Course in Financial Mathematics (request access at http://www.comap.com/FloydVest/index.ht ml) This is a free course in financial mathematics for upper high school and undergraduate students, with emphasis on personal finance.	
		Financial Math Financial Math Comprehensive Curriculum Units 1- 5 Black Line Masters Financial Math Units 6-10 5 Black Line Masters Financial Math	
		Task(s) Math Vision Project: Linear and Exponential Functions Task 5: Getting Down to Business GSE Algebra II/ Advanced Math: Unit 5 Exponential and Logarithmic Functions	
		Exponential and Logarithmic Functions How Does Your Money Grow? p. 86 SCS Finite Math Task: Compound Interest SCS Finite Math Task: Bonds SCS Finite Math Task: Amortization	



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RESOURCE TOOLBOX				
Textbook Resources	Standards	Videos		
Advanced Algebra & Trigonometry (Coburn)	Common Core Standards - Mathematics Common Core Standards - Mathematics Appendix A	Khan Academy Illuminations (NCTM)		
Algebra & Trigonometry (Blitzer)	http://www.ccsstoolbox.org/ Common Core Lessons	Discovery Education The Futures Channel The Teaching Channel		
Elementary Statistics Textbook (Bluman)	Tennessee Mathematics Standards	Teachertube.com		
Elementary Statistics 7th edition Bluman (PowerPoints, Chapter PDF files, Solutions Manual, etc.)		FiniteHelp Lecture Videos APStats Guy Against All Odds Videos (with Study Guides) (A Video Series that introduces a statistical topic and illustrates it with a real-world		
Stats Modeling the World		example)		
Tennessee Finite Math (Maki & Thompson)				
Calculator	Interactive Manipulatives	Additional Sites		
Texas Instruments Education	Stat Trek	NCTM Math Illuminations		
<u>TI-Nspired</u>	Rossmanchance.com	Math is Fun		
http://www.atomiclearning.com/ti_84		Wolfram Math World		
<u>TICommonCore.com</u>	ACT	Stat Trek		
http://www.casioeducation.com/educators	TN ACT Information & Resources	STatistics Education Web		
	ACT College & Career Readiness Mathematics Standards	Accelerated GSE Pre-Calculus Tasks: Unit 9-Probability		
		http://www.edutoolbox.org/tntools (formerly tncore.org)		